

ALGEBRA I REGENTS 2023 CHEAT SHEET

Be calm. Make the test work for you. Look for like/similar questions. Rewrite the question to take out the info that you need.

NEED-TO-KNOW VOCABULARY

ORDER OF OPERATIONS - PEMDAS

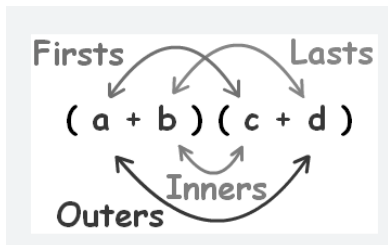
	<i>ex:</i> $25 - 4^2 + 3 * 4$
Parenthesis	no parenthesis in this problem
Exponents	$25 - 16 + 3 * 4$
Multiply/Divide	$25 - 16 + 12$
Add/Subtract	$9 + 12$
Solution	21

ALGEBRA

Constant	the term that doesn't change	<i>ex:</i> $2m + \underline{7}$
Coefficient	the number attached to the letter	<i>ex:</i> $\underline{2}m + 7$
Variable	any term with a letter	<i>ex:</i> $2m + 7$
	Combining Like Terms <i>ex:</i> $3m + 2b + 12m - 5b = 15m - 3b$ ★ be sure to use symbol in front of coefficient when combining	
Ratio	comparison of two numbers	<i>ex:</i> $\frac{3}{4}$ or 3:4
Exponents	the power/degree, how many times to multiply the base number	<i>ex:</i> 5^3 (3 = exponent)
Base	the number that gets multiplied by itself	<i>ex:</i> 5^3 (5 = base) <i>ex:</i> To solve $(5 * 5 * 5) = 125$

FOIL METHOD FOR MULTIPLYING TWO BINOMIALS

FOIL	First - Outer - Inner - Last	working with trinomials
------	------------------------------	-------------------------



NAMES FOR DIFFERENT TYPES OF TOTALS, ANSWERS, OR SOLUTIONS

Sum	a result after adding two or more numbers	<i>total, add</i>
Difference	a result after subtracting two or more numbers	<i>less than, minus, subtract</i>
Product	a result after multiplying two or more numbers	<i>factor, of</i>
Quotient	a result after dividing two or more numbers	<i>dividing</i>
Absolute Value	distance from zero	★ value is always positive (+)

COORDINATE PLANE AND FUNCTIONS

Function (FNC)	a relationship between x and y	for each <i>x-value</i> , there is only one <i>y-value</i> (no repeating <i>x-value</i>)
Domain	x- value	(x , y)
Range	y- value	(x, y)
Line Formula	$y = mx + b$	m =slope, b = y-intercept
Point Slope	$y - y_1 = m(x - x_1)$	
Slope Formula	$m = \frac{y_2 - y_1}{x_2 - x_1}$	<i>rise over run</i>
Y-Intercept	where the line intersects y axis	b value (start here when making a line)
Linear FCN	points make a line, constant rate of change	
Non-Linear FCN	does not look like a line	<i>ex: parabola, repeating x-values</i>
Quadratic FCN	make parabolas	<i>smile-y face or frowny face</i>
Exponential	upward sloping, y-value increases faster than the x, always lies above the x-axis	
Sequence	a type of function used to describe patterns	

EXPONENT RULES

Multiplying: When multiplying exponents with the same base, we add the exponents	$ex: 5^3 * 5^3 = 5^{3+3} = 5^6$
Dividing: When dividing exponents with the same base, we subtract the exponents	$ex: 2^3 \div 2^2 = 2^{3-2} = 2^1 = 2$ ★ Note: anything to the $^1 =$ invisible
Raising to another power: We will multiply the exponents, when raising the base to another power	$ex: (2^3)^3 = 2^{3*3}$ $3*3 = 2^9 = 2 * 2 * 2 * 2 * 2 * 2 * 2 * 2 * 2 = 256$ ★ any base to the 0 (zero power) = 1 $ex: 2^0 = 1, 10^0 = 1, x^0 = 1$
Negative exponents: Neg. exponents in the numerator, become a positive exponent in the denominator	$ex: 4^{-3} = \frac{1}{4^3} = \frac{1}{64}$

QUADRATIC EQUATIONS

How to solve	Set equation equal to zero, then break polynomial into 2 factors: () ()												
	<table border="0" style="width: 100%;"> <tr> <td style="text-align: center;">$ex: x^2 + 5x + 6 = 0$</td> <td style="text-align: right;">Look for factors of 6, that when combined together will give us the middle term of 5.</td> </tr> <tr> <td style="text-align: center;">$(x + 3)(x + 2) = 0$</td> <td style="text-align: right;">Solve each quantity individually for x</td> </tr> <tr> <td style="text-align: center;">$x + 3 = 0$</td> <td style="text-align: center;">$x + 2 = 0$</td> </tr> <tr> <td style="text-align: center;">$-3 \quad -3$</td> <td style="text-align: center;">$-2 \quad -2$</td> </tr> <tr> <td style="text-align: center;">$x = -3$</td> <td style="text-align: center;">$x = -2$</td> </tr> <tr> <td></td> <td style="text-align: right;">Our two solutions for x are -3 and -2</td> </tr> </table>	$ex: x^2 + 5x + 6 = 0$	Look for factors of 6, that when combined together will give us the middle term of 5.	$(x + 3)(x + 2) = 0$	Solve each quantity individually for x	$x + 3 = 0$	$x + 2 = 0$	$-3 \quad -3$	$-2 \quad -2$	$x = -3$	$x = -2$		Our two solutions for x are -3 and -2
$ex: x^2 + 5x + 6 = 0$	Look for factors of 6, that when combined together will give us the middle term of 5.												
$(x + 3)(x + 2) = 0$	Solve each quantity individually for x												
$x + 3 = 0$	$x + 2 = 0$												
$-3 \quad -3$	$-2 \quad -2$												
$x = -3$	$x = -2$												
	Our two solutions for x are -3 and -2												
How to FOIL given 2 quantities	Basically, you are using the distributive property twice. $ex: Given (x + 4) (x - 5) =$												
	<table border="0" style="width: 100%;"> <tr> <td style="text-align: center;">First: $x \cdot x = x^2$</td> <td style="text-align: right;">first term in 1st () times 1st term in 2nd ()</td> </tr> <tr> <td style="text-align: center;">Outer: $x \cdot (-5) = -5x$</td> <td style="text-align: right;">x from 1st () -5 from the 2nd ()</td> </tr> <tr> <td style="text-align: center;">Inner: $4 \cdot x = 4x$</td> <td style="text-align: right;">4 from the 1st () times x from the 2nd ()</td> </tr> <tr> <td style="text-align: center;">Last: $4 \cdot (-5) = -20$</td> <td style="text-align: right;">4 from 1st () times -5 from the 2nd ()</td> </tr> <tr> <td colspan="2" style="text-align: center;">Combine all terms: $x^2 - 5x + 4x - 20 = x^2 - 1x - 20$</td> </tr> </table>	First: $x \cdot x = x^2$	first term in 1 st () times 1 st term in 2 nd ()	Outer: $x \cdot (-5) = -5x$	x from 1 st () -5 from the 2 nd ()	Inner: $4 \cdot x = 4x$	4 from the 1 st () times x from the 2 nd ()	Last: $4 \cdot (-5) = -20$	4 from 1 st () times -5 from the 2 nd ()	Combine all terms: $x^2 - 5x + 4x - 20 = x^2 - 1x - 20$			
First: $x \cdot x = x^2$	first term in 1 st () times 1 st term in 2 nd ()												
Outer: $x \cdot (-5) = -5x$	x from 1 st () -5 from the 2 nd ()												
Inner: $4 \cdot x = 4x$	4 from the 1 st () times x from the 2 nd ()												
Last: $4 \cdot (-5) = -20$	4 from 1 st () times -5 from the 2 nd ()												
Combine all terms: $x^2 - 5x + 4x - 20 = x^2 - 1x - 20$													

THE NUMBER SYSTEM

REAL

includes all the numbers

- A. Irrational numbers that cannot be written as a fraction, never end and never repeat *ex: π or $\sqrt{2}$*
- B. Rational can be written as a fraction or a decimal that ends or repeats. *ex: 0.3333 or 0.25*
- I. Integers: whole numbers and their opposites *ex: 4 and -4*
- II. Whole: start with 0 *ex: 0, 1, 2, 3 ...*
- III. Natural: where one naturally wants to start counting *ex: 1, 2, 3 ...*

PROPERTIES

Commutative	with addition and multiplication of numbers, you can change the order of the numbers in the problem, and it will not affect the answer.	<i>ex: $a + b = b + a$</i>
Distributive	number outside property is multiplied by all terms inside properties	<i>ex: $2(3+4) = (2*3)+(2*4)$</i>
Associative	values inside of the parenthesis change / grouping changes	<i>ex: $(a+b)+c = a+(b+c)$</i>
Identity (Addition)	add any number to zero, the number stays the same ★ also called the Zero Property	<i>ex: $a+0 = a, 9+0 = 9$</i>
Identity (Multiplication)	anything times one is the number	<i>ex: $5*1 = 5$</i>
Equation vs. Expression	equations have = expressions are just phrases	
Inequalities	a phrase is greater than ($x > 1$), less than ($x < 1$), (\leq) less than or equal to, or (\geq) greater than or equal to.	

STATISTICS

Mean	the average of the values	sum of values, divided by how many values there are. <i>a.k.a. Fair value</i>
Median	middle value	★ arrange the data points smallest to largest , find the middle number
Range	largest value minus smallest value	
Mode	the value that occurs most frequently	<i>most</i>
Quartile	three identifiers in which the data set can be grouped	<i>ex: Q1, Q2 (same as median), Q3</i>
Interquartile Range (IQR)	a way in which to measure the spread of data	<i>ex: Q3 – Q1</i>
Square Root	the reverse of a squared number (a number multiplied by itself to get that number)	
Cubed Root	the reverse of a cubed number (a number multiplied by itself three times to get that number)	

TI – 84

Turn on:

- Clear all : 2nd → + → 7 → 1 → 2
- Input Data for tables:
Stat → Edit → Enter
- To clear: ↑ *clear* ↓
- Insert data to get a linear regression:
x-values = L1, y-values = L2 → *stat* → *calc* → #4 → *enter*
- Input data for tables

Reference Sheet for Algebra I (NGLS)

Conversions

1 mile = 5280 feet
 1 mile = 1760 yards
 1 pound = 16 ounces
 1 ton = 2000 pounds

Conversions Across Measurement Systems

1 inch = 2.54 centimeters
 1 meter = 39.37 inches
 1 mile = 1.609 kilometers
 1 kilometer = 0.6214 mile
 1 pound = 0.454 kilogram
 1 kilogram = 2.2 pounds

Quadratic Equation	$y = ax^2 + bx + c$
Quadratic Formula	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
Equation of the Axis of Symmetry	$x = -\frac{b}{2a}$
Slope	$m = \frac{y_2 - y_1}{x_2 - x_1}$
Linear Equation Slope Intercept	$y = mx + b$
Linear Equation Point Slope	$y - y_1 = m(x - x_1)$

Exponential Equation	$y = ab^x$
Annual Compound Interest	$A = P(1 + r)^n$
Arithmetic Sequence	$a_n = a_1 + d(n - 1)$
Geometric Sequence	$a_n = a_1r^{n-1}$
Interquartile Range (IQR)	$IQR = Q_3 - Q_1$
Outlier	Lower Outlier Boundary = $Q_1 - 1.5(IQR)$
	Upper Outlier Boundary = $Q_3 + 1.5(IQR)$