

Problem O







Problem J







Problem A.



$$\frac{9}{10} = 0.9$$

How many ONES? (0) How many tenths? (9) How many hundredths? (0) Problem B.

ONES	tenths	hundredths
		0 ם ם ם ם ם ס
0.		6

O. QP 6 100 =

How many ONES? (0) How many tenths?(0) How many hundredths? (units) (8)





	1	2	3	4	5	6	7	8	9	10	11	12	13	
1														
2														
3														
4														
5														
6														
7														
8														
9														
10														
11														
12														
13														

Problem D: Solving 13 by 13 with an array and another way.

Graphing explained: 13 x 13 = (10 + 3) x (10 + 3) (When graphing, start with the largest place value, the TENS place in this example.)	Another method to multiply. (without the shortcut of carrying or regrouping) Note: Students can carry & regroup and other methods of working it out.				
10 rows x 10 columns = 100 units	<i>Think:</i> 13 = 10 + 3				
3 rows x 10 columns = 30 units	13 (Start with the ONES place) X 13				
3 columns x 10 rows = 30 units	9 (3 ones x 3 ones = 9) 30 (3 ones x 1 ten (10) = 30)				
Count the single squares left = 9 units	30 (1 ten (10) x 3 ones = 30) <u>+ 100</u> (1 ten (10) x 1 ten (10) = 100)				
100 + 30 + 30 + 9 = 100 + 60 + 9 = 169 units	169				

Problem E: Solving 11 by 13 with an array and another way.

	1	2	3	4	5	6	7	8	9	10	11	12	13	
1												-		
2														
3														
4														
5														
6														
7														
8														
9														
10														
11												-		
12														
13														

Graphing explained: **One other method to multiply.** (without the $11 \times 13 = (10 + 1) \times (10 + 3)$ *shortcut of carrying or regrouping)* (When graphing, start with the largest place value, *Note: Students can also carry & regroup and other* the TENS place in this example.) methods of working it out. 10 rows x 10 columns = 100 units *Think:* 11 = (10 + 1) 13 = (10 + 3)1 rows x 10 columns = 10 units 11 (Start with the ONES place) X 13 3 columns x 10 rows = 30 units 3 (3 ones x 1 one = 3) 30 (3 ones x 1 ten (10) = 30) Count the single squares left = 3 units 10 (1 ten (10) x 1 one = 10) + 100 (1 ten (10) x 1 ten (10) = 100) 100 + 10 + 30 + 3 =143 100 + 40 + 3 = **143 units**

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1															
2															
3															
4															
5															
6															
7															
8															
9															
10															
11					-		-								
12															
13															

Problem F: Solving 13 by 15 with an array and another way.



Graphing explained: 13 x 15 = (10 + 3) x (10 + 5) (When graphing, start with the largest place value, the TENS place in this example.) 10 rows x 10 columns = 100 units

3 rows x 10 columns = 30 units

5 columns x 10 rows = 50 units

Count the single squares left = 15 units

100 + 30 + 50 + 15 = 100 + 80 + 15 = 100 + 95 = **195 units** **One other method to multiply.** (without the shortcut of carrying or regrouping) Note: Students can also carry & regroup and other methods of working it out.

Think: 13 = 10 + 3 15 = 10 + 5

15 (Start with the ONES place)

15 (3 ones x 5 ones = 15)

30 (3 ones x 1 ten (10) = 30)

50 (1 ten (10) x 5 ones = 50)

195



Problem H. Arrange (0.56 and 0.7 from largest to smallest

- A student might look at the numbers, ignore the decimal point and think "56" is larger than "7"
- Have student draw the decimals or count out the paper rods for tenths and draw the hundredth place.
- The ONES place has the largest value does one number have more ONES? (no)
- The tenths place has the next largest value does one number have more tenths? (yes 0.7 that is the larger decimal)



ONES	tenths	hundredths

WHALE Sample Solutions (June 2022)





Problem P. Write the Fact Family for this array.

How many rows? (5) How many columns? (4) How many units altogether inside ? (20) Fact Family: $5 \times 4 = 20$ $4 \times 5 = 20$



Problem Q. $? \div 6 = 4$ (if student needs to figure this out) What starts the Fact Family in division? (**The product/total # inside the array**) What are 6 & 4 in the array? (**one is the # of rows; the other is the # of columns.**) What do you want to use for the rows? 6 or 4? Set up the array and count the units inside. What is the missing number? (24) ($24 \div 6 = 4$)



Problem R. $40 \div ? = 8$ (if student needs to figure this out) Do we have the Product/ total # inside the array for this Fact Family? (yes)

So in an array, Do you want the "8" to be the rows or columns?

- If student chooses columns, have student number the columns 1 8. (see sample above)
- Now figure out how many rows by counting the units in each row, or skip counting by 8's up to 40.
- How many rows are needed? (5) The missing number is
 5 (40 ÷ 5 = 8)
- *If the student chooses ROWS*, then have the student number the rows 1 -8 and go and then fill in the columns one at a time until count to 40.

		2	3	Ч	5	
	X	×	×	X	×	בל - סוו
2	×	×	X	×	X	40
3	X	X	X	X	X	
4	X	×	×	×	×	
5	×	X	X	×	X	
b	×	X	X	×	X	
2	X	×	×	X	X	De ce O
5	X	X	x	X	X	Page 9





Problem B.







8

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Problem D. ___ x 7 = 56 (If student needs assistance)
Thinking about Fact Families and arrays, what is missing? The
for rows or the total product? (row)

- Start an array with 7 columns.
- Need to figure out how many rows by counting each unit in each row.
- What total are we trying to reach? (56)
- How many rows did we need to get to 56? (8)
- The missing number is <u>8</u>. (<u>8</u> x 7 = 56)

Problem E. ____ ÷ 7 = 9 (if student needs help)
Thinking about Fact Families and arrays, what is missing? The # for rows or the total product? (total product).

• Which number do you want to use for the rows? 9 or 7? (this sample uses 7 rows)

6

5

- Number the rows and columns, then count.
- The product total is? (63) 63 ÷ 7 = 9







Problem F. ____ ÷ 7 = 7 (if student needs help)

Thinking about Fact Families and arrays, what is missing? The # for rows or the total product? (total product)

- What number do you want for the rows? (has to be 7!)
- Number the rows and columns, then count.
- (depending on the student) Is there a fast way to know 5 x 7, so we don't have to count every square?
- Do you know what 5 x 7 is? Or count by 5's to figure it out?
- So we can just box 5 x7 because we know that 5 x 7 equals...? (35)
- And start counting from 35 for the last two rows.
- The total is... (49) 49 ÷ 7 = 7



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Do you want to make 4 rows with 5 columns or 5 rows with 4 columns?

- Officially, the first factor tells the number of rows or groups in the problem. This can help students decode word problems.
 - o 4 rows of 5
 - o 4 groups of 5
- In this case, however, the communitive law for mulitiplication works: (4 x 5) = (5 x 4)

Ask student to use the array graphic organizer to draw to show 5 \times 4

*Not required from the question, but still ask:

• What does 5 x 4 equal? (20)



E. What's missing? ____ ÷ 7 = 9 If student needs help: What is missing? The row or product total? (product/total)

• How can we use the factors 7 and 9 to find out the product or total?

• (multiply 7 x 9; skip count; make an array) Making an Array: Write numbers to show 7 rows and 9 columns.

Do you know, or can you figure out, what 5 x 9 equals? (45)

- Find the 7 rows and make a block for 5 x 9.
- Write "45" instead of counting every square.

Do you know what 2 x 9 equals? (18)

• Now that we know one chunk equals 45 and the other part equals 18, what can we do? (Add: 45 + 18 = ?)



↔ WHALE Sample Solutions (June 2022)





Problem I: Write decimal for 2/100

- Are there any ONES? (no)
 - Write "0" in the ONES place.
- How many tenths are there?(none, 0)
 - $\circ~$ Write "0" in the tenths place.
- How many hundredths, or units are there? (2)
 - Draw 2 units in the hundredths place and write the number "0"
- How do you write the decimal?





J. Write decimal for ³/₄.

If student needs help:

- To find the decimal
 - We can divide the numerator (3) by the denominator (4), or
 - $\circ~$ Figure out if the denominator (4 ths) has an equivalent fraction in 10 $^{ths}~$ or 100 ths .

If looking for equivalent 10th or 100th,

- Do "fourths" have an equivalent fraction to tenths? Does 4 x (anything) = 10? (no)
- Do fourths have an equivalent fraction to hundredths? Does 4 x (anything) = 100? How about 4 quarters? Do 4 quarters make \$1.00? or 100 cents? (yes)

Since 4 x 25 = 100, let's figure out how many hundredths 3 fourths make:

$$\frac{3}{4} \times \frac{25}{25} = \frac{75}{100} = 0.75$$